

Honoring the past  
Celebrating the present  
Preparing for the future  
Houston, Texas • July 27 - 31, 2008

CELEBRATE 50 YEARS  
AAPM

Tuesday, July 29<sup>th</sup> 2008  
8:30 AM – 9:25 AM

## Deformable Image Registration: Methods and Endpoints

M

Marc L Kessler, PhD  
The University of Michigan

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Tuesday, July 29<sup>th</sup> 2008  
8:30 AM – 9:25 AM

By 9:25 AM, you will be able to ...

- ✓ Describe the basic mechanics (*recipes*) of image registration techniques used in commercial & research planning and delivery systems
- ✓ Describe the different techniques used to combine, display & interact with multimodality and 4D image data
- ✓ Understand the clinical use & application of these techniques for treatment planning, treatment delivery & plan adaptation


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8:30 AM – 9:25 AM

What's the *recipe* for registering and fusing 3D & 4D image data?

What's the *cake*?



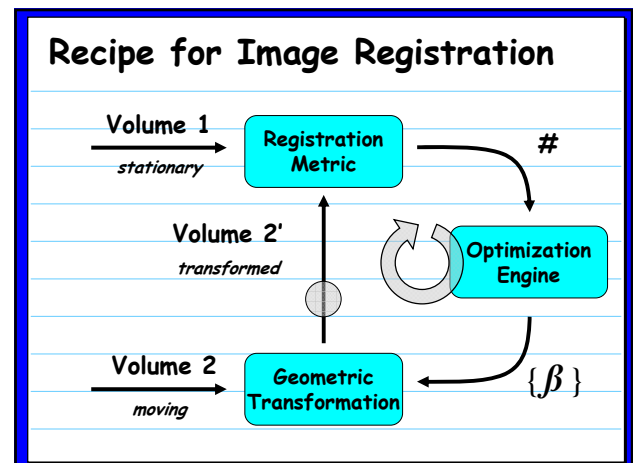
## The Recipe

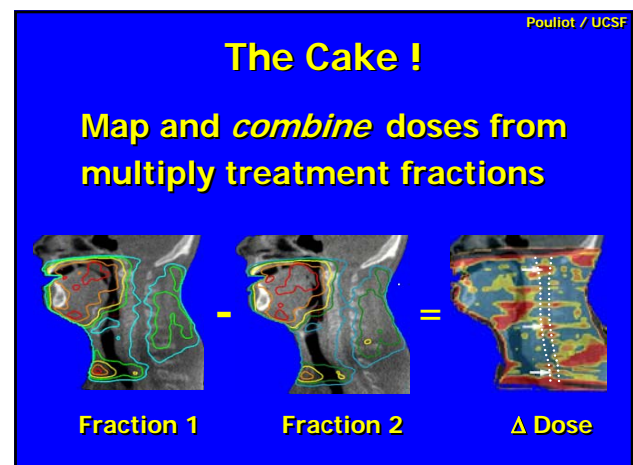
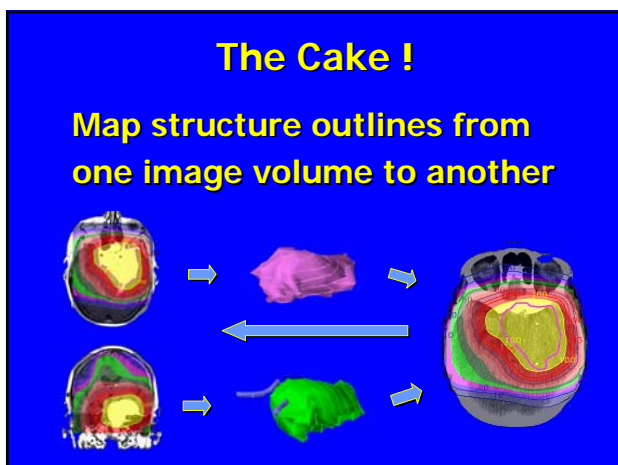
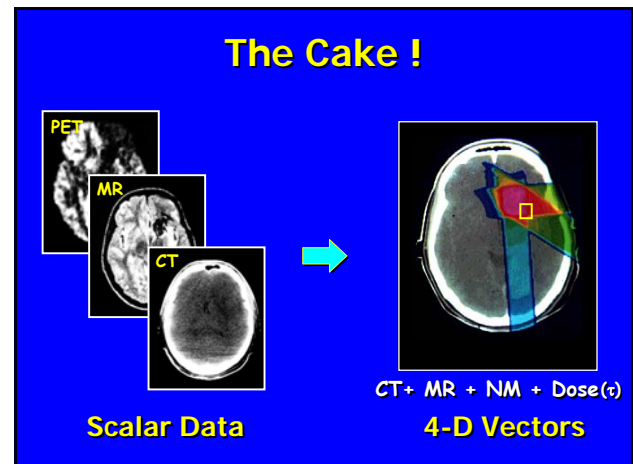
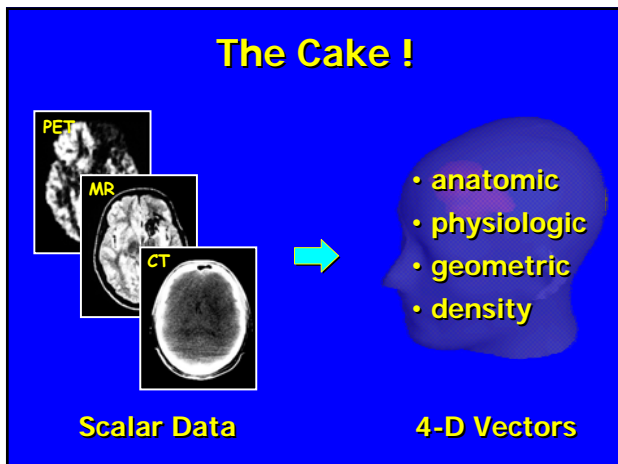
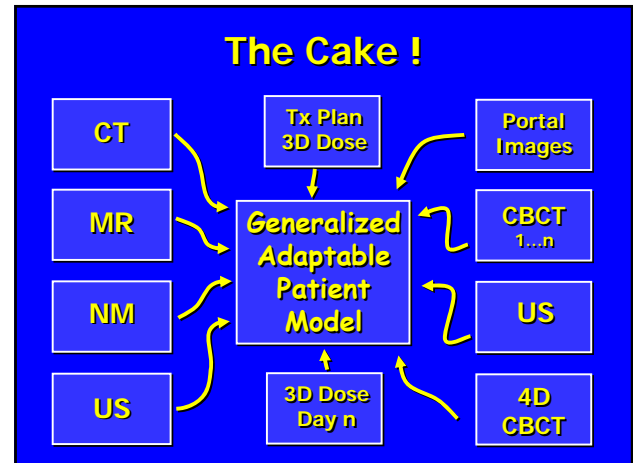
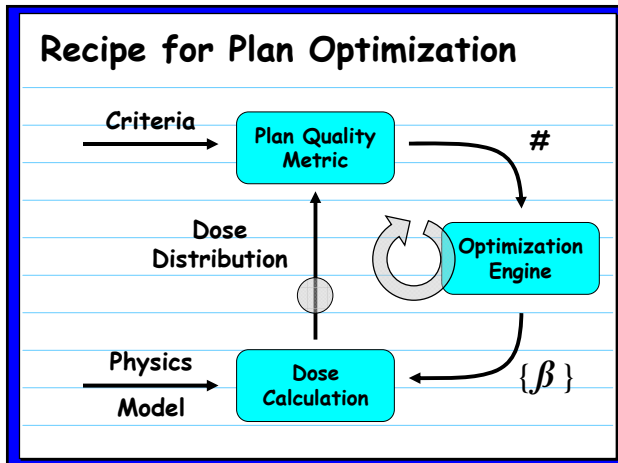


Recipe for Image Registration
2 Image Volumes
1 Transformation Model
1 Registration Metric
1 Optimization Engine
n Evaluation Tools

### Recipe for Image Registration

2 Image Volumes
1 Transformation Model
1 Registration Metric
1 Optimization Engine
n Evaluation Tools





## Deformable Image Registration Methods and Clinical Endpoints

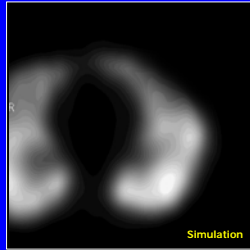
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## The Cake !

### Dose – Function Analysis



Planning CT



SPECT Imaging

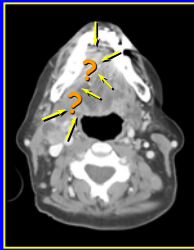
## Recipe for Image Registration

→ 2 Image Volumes

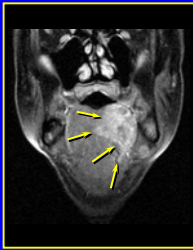
*Chose 2 from the plethora of  
imaging volumes we now have  
available in radiation therapy!*

## Available Image Volumes

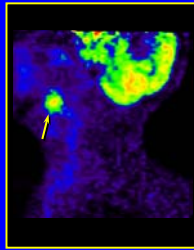
Gregoire / St-Luc



PhysiCS



Anatomy

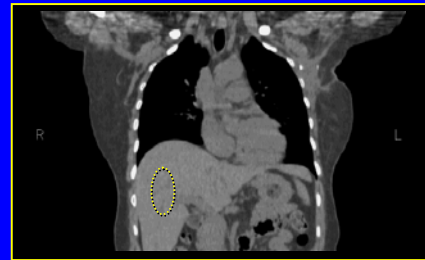


Physiology

*...multiple modalities*

## Available Image Volumes

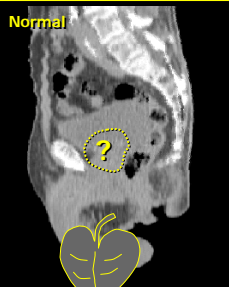
Balter / UM



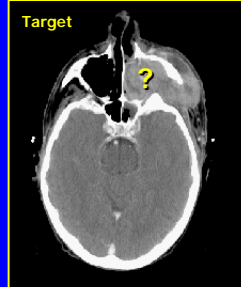
Motion Information

*...4-D imaging*

## Available Image Volumes



Normal



Target

*...repeat imaging during therapy*

## Available Image Volumes

Dawson / PMH



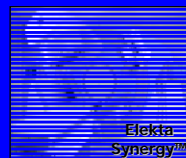
Varian  
OBI™



Siemens  
PRIMATOM™



ViewRay  
Renaissance™



Elekta  
Synergy™



Tomotherapy  
Hi-Art™



Resonant  
Restitu™

*...at the treatment unit too!*

# Deformable Image Registration Methods and Clinical Endpoints

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## Recipe for Image Registration

2 Image Volumes

*Depending on the application,  
choose either entire volumes  
or the relevant sub-volumes*

## Prostate Example

*Can you tell what is different in the 2 volumes?*



Volume 1

Volume 2

## Prostate Example

*Bones aligned, prostate region not aligned*



*Entire Volume*

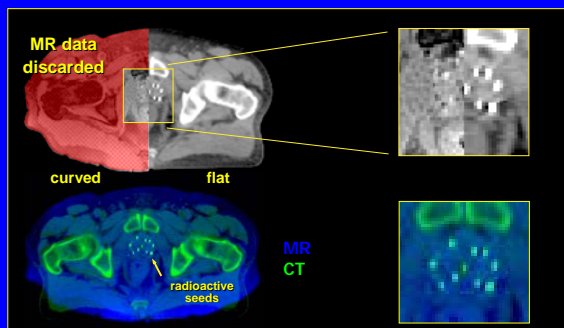
## Prostate Example

*Bones ignored, prostate region aligned*

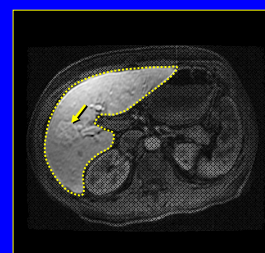


*Sub volumes*

## Prostate Example



## Liver Example



*anatomic-based  
cropping*



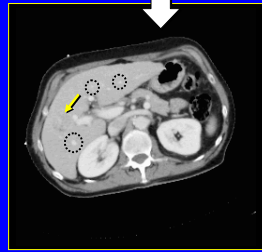
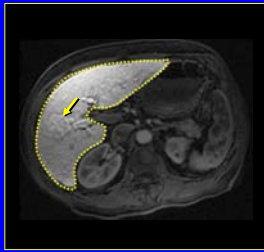
*ignore anatomy  
outside liver*

# Deformable Image Registration Methods and Clinical Endpoints

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## Liver Example

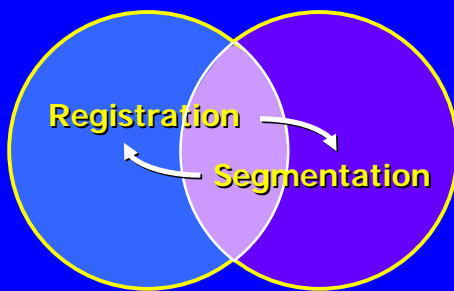


## The Past / Present

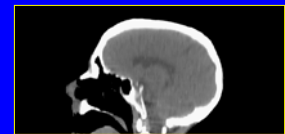
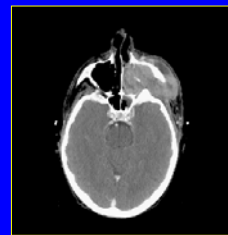
Registration

Segmentation

## The Present / Future



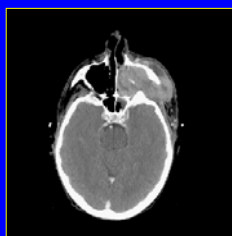
## Treatment Delivery Example



Rigid assumption used for regional registration

Pick Your Battles Wisely!

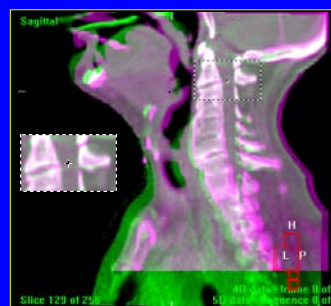
## Treatment Delivery Example



Oops!

## Registration at Delivery

Sonke / NKI



Regional registration of serial CBCT scans and TP CT

6 DOF

Choose your battles wisely!

# Deformable Image Registration Methods and Clinical Endpoints

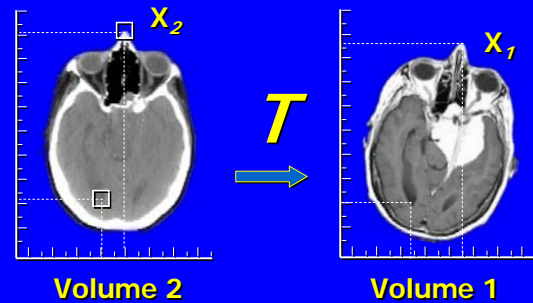
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## Recipe for Image Registration

### 1 Transformation Model

*Depending on the input data  
and clinical situation, chose  
a transformation model*

## Transformation Model



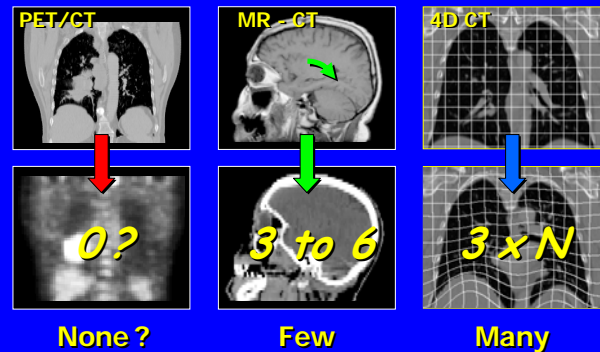
## Recipe for Image Registration

### → 1 Transformation Model

$$X_1 = T(X_2, \{\beta\})$$

Choose the flavor of  $T$  and  
the set of parameters  $\{\beta\}$

## Degrees of Freedom $\{\beta\}$



## Available Flavors of $T$

### ➤ Rigid / Affine

*... or regional rigid / affine*

### ➤ Full 3D / 4D Deformation

*Parametric transformations*

*Free-form transformations*

## Available Flavors of $T$

### Affine Assumption

$$y = mx + b \quad \dots \text{in three dimensions}$$

$$x_1 = A x_2 + b \quad \dots \text{up to 12 DOF}$$

### Otherwise

#### Spatially variant transformations

Various parametric & free form models  
*... up to  $3 \times N$ !*  
*... lots of degrees of freedom!*

# Deformable Image Registration Methods and Clinical Endpoints

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www.gnome.org

## Affine Transformations

Volume 2

A Square

Rotation

3

Translation

3

Scaling

3

Shearing

3

Volume 1

**Parallel lines *stay* parallel!**

www.gnome.org

## Affine Transformations

Volume 2

**6 DOF**

Rotation

3

Translation

3

**Parallel lines *stay* parallel!**

Munro / Varian

## Affine Transformations

**3 or 4 DOF**

Machine Values	TARGET	ACTUAL	SHIFT	
Couch Lat	997.8	998.6	-0.8	<input checked="" type="checkbox"/> Include
Couch Lng	85.2	85.0	0.2	<input checked="" type="checkbox"/> Include
Couch Vrt	999.6	0.5	-0.9	<input checked="" type="checkbox"/> Include
Couch Rtn	0.0	0.0	0.0	<input checked="" type="checkbox"/> Include

**Parallel lines *stay* parallel!**

www.gnome.org

## Affine Transformations

Rotation

Translation

Scaling

Shearing

**Parallel lines *stay* parallel!**

## non-Affine Transformations

Volume 1

Volume 2

**Parallel lines *don't* stay parallel!**

## non-Affine Transformations

Volume 1

Volume 2

$$\mathbf{x}_1 = \mathbf{T}(\mathbf{x}_2, \{\beta\})$$

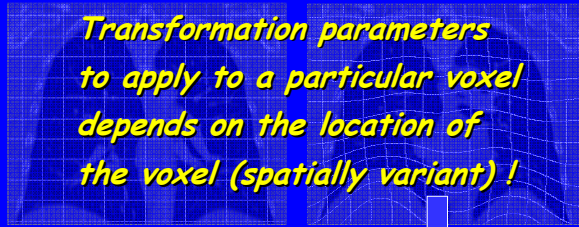
# Deformable Image Registration Methods and Clinical Endpoints

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## non-Affine Transformations

Study A

Study B



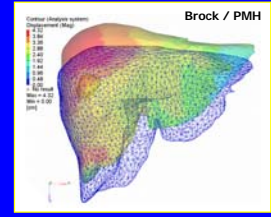
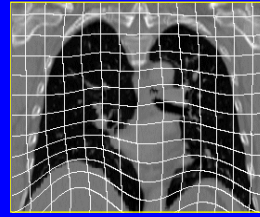
*Transformation parameters  
to apply to a particular voxel  
depends on the location of  
the voxel (spatially variant) !*

$$X_1 = T(X_2, \{\beta(X_2)\})$$

## Available Flavors of $T$

Parametric Models

Freeform Models



Warp Space /  
... Drag Objects

Warp Objects /  
... Drag Space

## Available Flavors of $T$

Spatially variant transformations

➤ Parametric

Thin-plate Splines

Global Deformations

B-Splines

Local Deformation

## Available Flavors of $T$

Spatially variant transformations

➤ Free Form

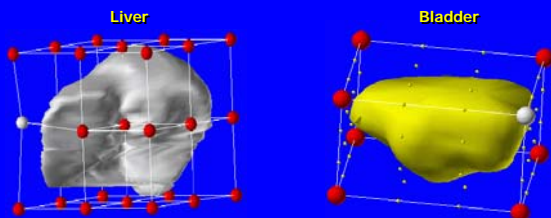
Intensity Flow Methods

Fluid Mechanics-like

Finite Element Models

Account for Physical Properties

## Thin-Plate Splines



$$T(P) = \underbrace{a_0 + a_x x + a_y y + a_z z}_{\text{affine}} + \underbrace{\sum_{i=1}^n w_i U(P - P_i)}_{\text{warping}}$$

## B-Spline Deformations

Each have some distinct properties

➤ B-Splines

$$\begin{aligned} X_2 &= X_1 + \Delta X \\ &= X_1 + \sum w_i B(X - k_i) \end{aligned}$$

$\nwarrow$  weights       $\swarrow$  basis function  
 ( ... parameters! )

# Deformable Image Registration Methods and Clinical Endpoints

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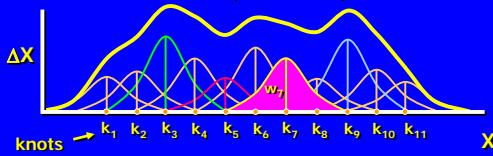


## B-Spline Deformations

Each have some distinct properties

### B-Splines

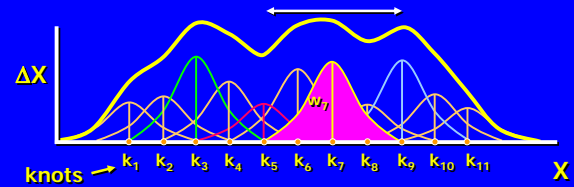
#### 1-D Example



$$X_2 = X_1 + \Delta X = X_1 + \sum w_i \cdot B(X-k_i)$$

## B-Spline Deformations

Construct overall function  $T$  from a weighted sum of local deformations

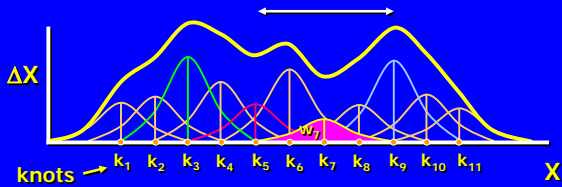


$$X_2 = X_1 + \Delta X = X_1 + \sum w_i \cdot B(X-k_i)$$

parameters!

## B-Spline Deformations

Construct overall function  $T$  from a weighted sum of local deformations

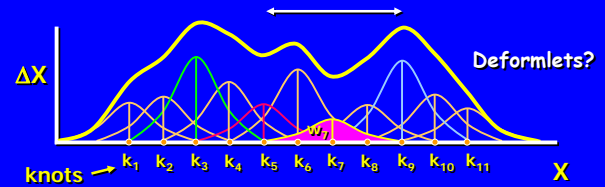


$$X_2 = X_1 + \Delta X = X_1 + \sum w_i \cdot B(X-k_i)$$

parameters!

## B-Splines

Construct overall function from a weighted sum of local deformations



$$X_2 = X_1 + \Delta X = X_1 + \sum w_i \cdot B(X-k_i)$$

This seems a lot like intensity modulation!

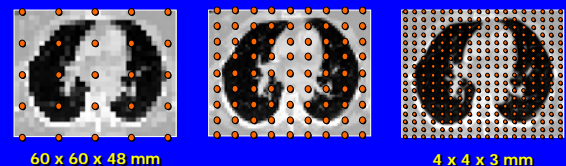
## B-Spline Transformation Model



3-D Grid of Knots

## Multiresolution Deformations

### Divide and Conquer



Coarse ➔ Fine  
Knot Spacing

# Deformable Image Registration Methods and Clinical Endpoints

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## Recipe for Image Registration

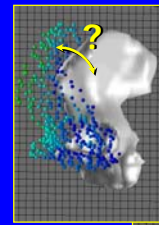
### ➡ 1 Registration Metric

Choose a registration metric

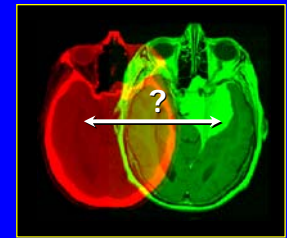
depending on the type of

imaging data involved

## Registration Metrics



Geometry-based



Intensity-based

## Geometry-Based Metrics

### ➤ Point Matching

Least Squares

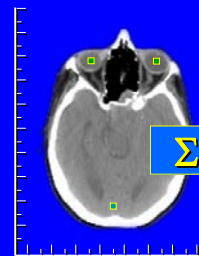
$$\sum (x_2 - x'_1)^2$$

### ➤ Surface Matching

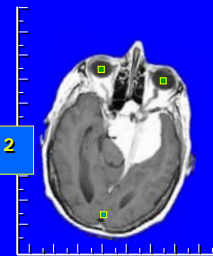
Chamfer Matching

$$\sum \min \text{distance}^2$$

## Point Matching



Volume 2

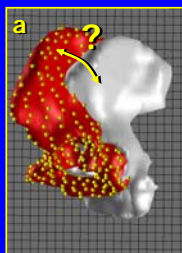


Volume 1

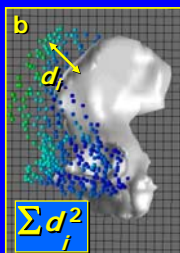
Define corresponding anatomic points

## Surface Matching

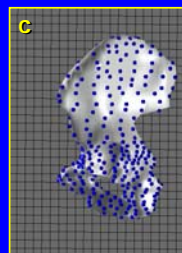
Catallo / UM



objects  
misaligned



compute  
mismatch

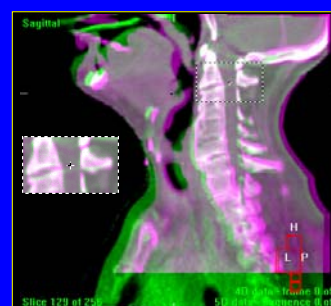


mismatch  
minimized

Define corresponding anatomic surfaces

## Registration at Delivery

Sonke / NKI



Regional  
registration  
of serial  
CBCT scans  
and TP CT

6 DOF

*Choose your battles wisely!*

# Deformable Image Registration Methods and Clinical Endpoints

Marc L Kessler, PhD

## Intensity-Based Metrics

### ➤ Mono-modality

Sum of Squared Diff.

$$\sum (I_2 - I_1)^2$$

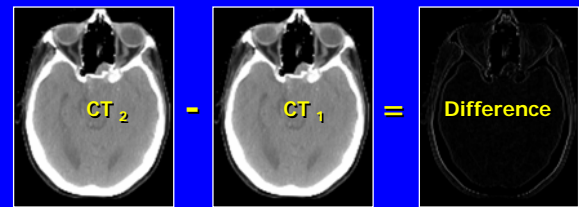
### ➤ Multimodality Data

Mutual Information

$$\sum p(A,B) \log \frac{p(A,B)}{p(A)p(B)}$$

## Sum of Squared Differences

... subtract one image from the other



$I_{CT_2}$

$I_{CT_1}$

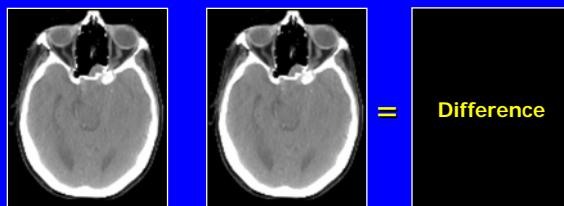
$\sum (I_{CT_1} - I_{CT_2})^2$

Individual Intensity Distributions

Sum of the Squares of the Differences

## Sum of Squared Differences

... subtract one image from the other



$I_{CT_2}$

$I_{CT_1}$

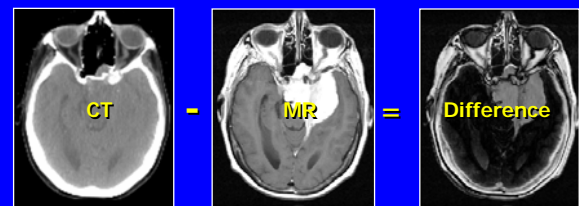
Zero

Individual Intensity Distributions

Registered

## Sum of Squared Differences

... subtract one image from the other



$I_{CT}$

$I_{MR}$

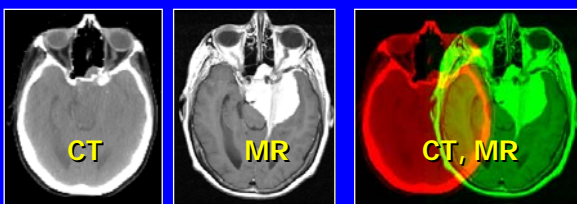
Not Zero

Individual Intensity Distributions

This doesn't usually make much sense

## Mutual Information

... using an information theory-based approach



$$H(I_{CT}) + H(I_{MR}) = H(I_{CT}, I_{MR}) ?$$

Individual Information Contents

Joint Information Content

## Mutual Information

$$H(I_1, I_2) = H(I_1) + H(I_2) - MI(I_1, I_2)$$

The mutual information is the information that is *common* to both image volumes!

'48 Shannon - Bell Labs / '95 Viola - MIT

# Deformable Image Registration Methods and Clinical Endpoints

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## Mutual Information

$$MI(I_1, I_2) = H(I_1) + H(I_2) - H(I_1, I_2)$$

The mutual information is the information that is *common* to both image volumes!

'48 Shannon - Bell Labs / '95 Viola - MIT

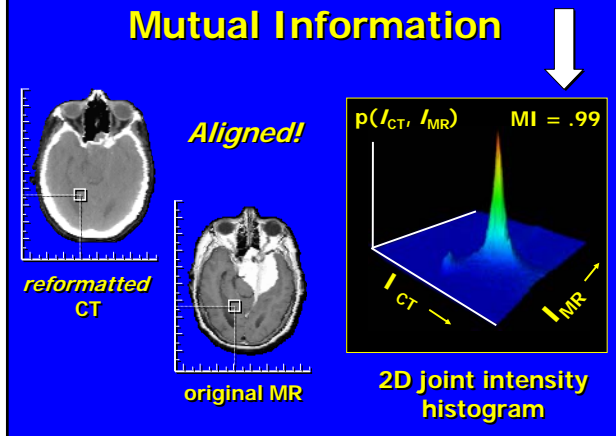
## Mutual Information

$$MI(I_1, I_2) = \sum p(I_1, I_2) \log_2 \left[ \frac{p(I_1, I_2)}{p(I_1) p(I_2)} \right]$$

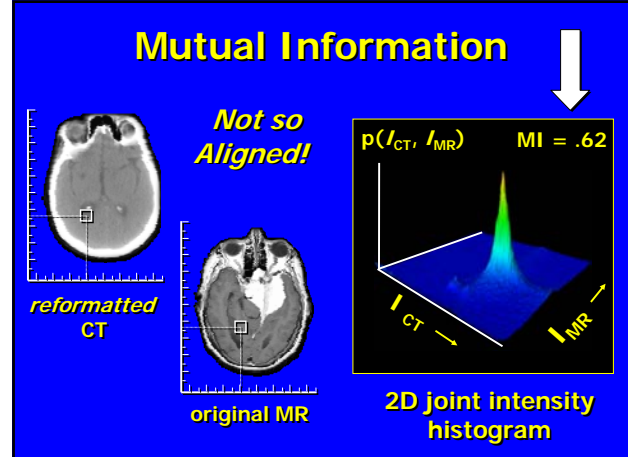
The mutual information of two image volumes is a maximum when they are *geometrically registered* ...

'48 Shannon - Bell Labs / '95 Viola - MIT

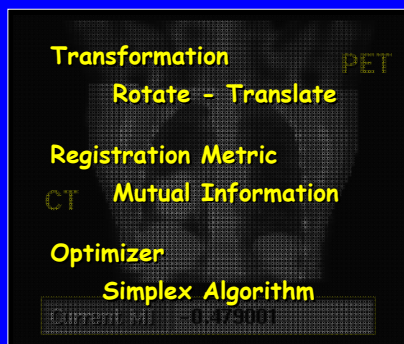
## Mutual Information



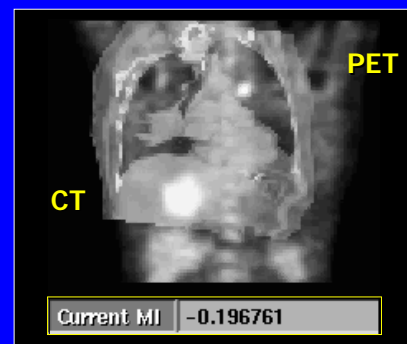
## Mutual Information



## How About An Example?



## How About An Example?

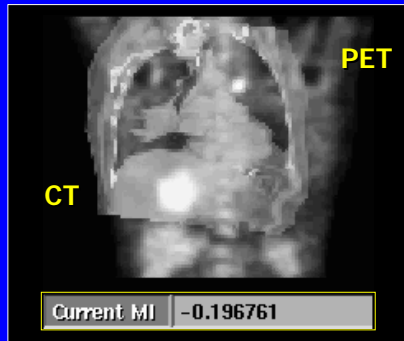


# Deformable Image Registration Methods and Clinical Endpoints

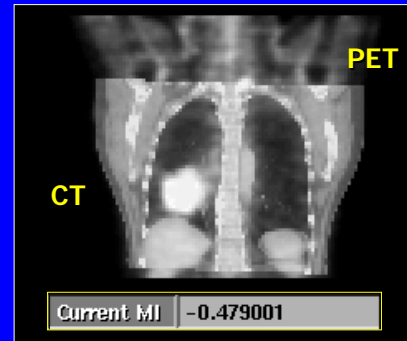
Marc L Kessler, PhD



## How About An Example?



## How About An Example?



### Recipe for Image Registration

2 Image Volumes

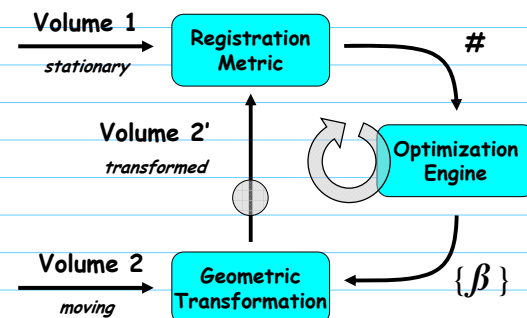
1 Transformation Model

1 Registration Metric

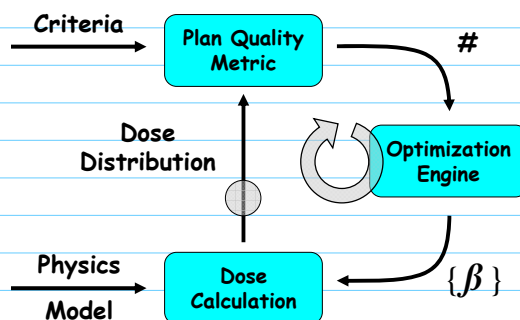
→ 1 Optimization Engine

n Evaluation Tools

### Recipe for Image Registration



### Recipe for Plan Optimization



## Interactive Registration



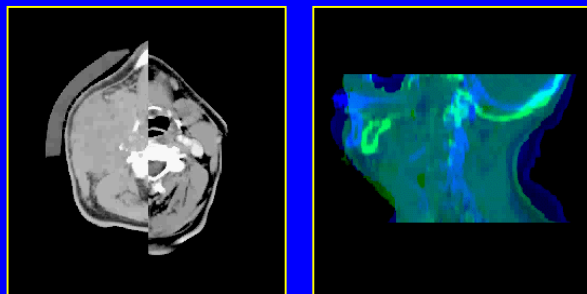
- ✓ Translate
- ✓ Rotate
- ? Deform

Provide tools to transform and visualize!

# Deformable Image Registration Methods and Clinical Endpoints

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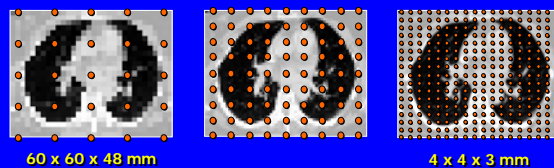
## Automated Registration



Rigid first , ... then B-Spline deformation

## Multiresolution Deformations

### Divide and Conquer



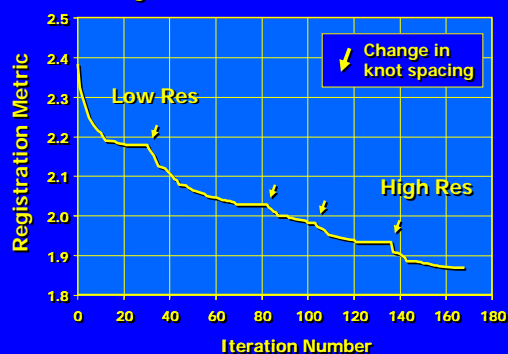
Coarse

Knot Spacing

Fine

## Multiresolution Deformations

Registration Metric vs. Iteration

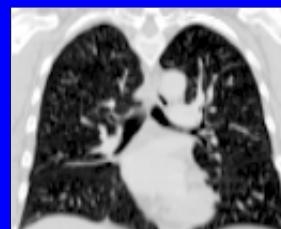


## Multiresolution B-Splines

ABC CT Example



Exhale State



Inhale State

## Multiresolution B-Splines

ABC CT Example



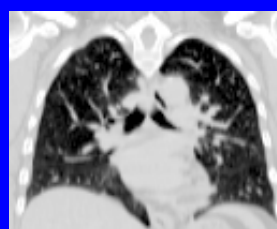
Exhale State



Inhale State  
deformed

## Multiresolution B-Splines

Multiphasic CT Data



Exhale State



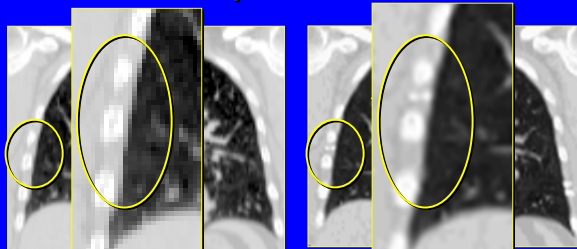
Inhale State  
deformed

# Deformable Image Registration Methods and Clinical Endpoints

Marc L Kessler, PhD

## Multiresolution B-Splines

Multiphase CT Data

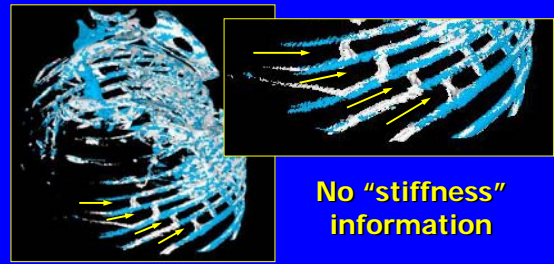


Exhale State

Inhale State  
deformed

## We Are Not *Really* Splines !

Ruan / UM



No "stiffness"  
information

Extracted Ribcage    ■ Exhale  
                             ■ Deform Inhale

## Add Some Physics?

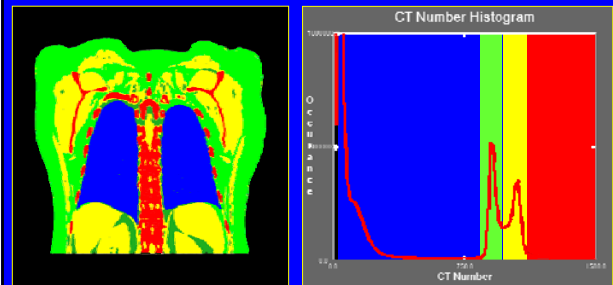
$$E_{total} = E_{similarity} + \alpha E_{stiffness}$$

intensity similarity metric

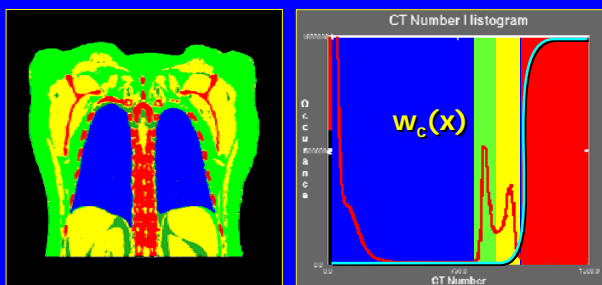
tissue-dependent regularization

$$E_{vol} = \int w_c(x) |\det J_T(x) - 1| dx$$

## Spatially Variant Stiffness

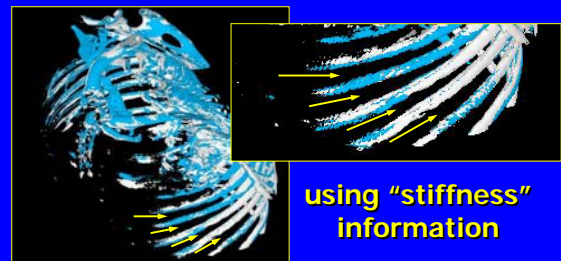


## "Stiffness" Weighting



## Using "Prior" Information

Ruan / UM



using "stiffness"  
information

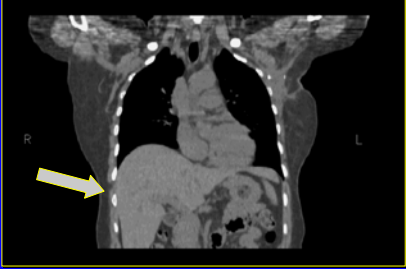
Extracted Ribcage    ■ Exhale  
                             ■ Deform Inhale

# Deformable Image Registration Methods and Clinical Endpoints

Marc L Kessler, PhD

Balter / UM

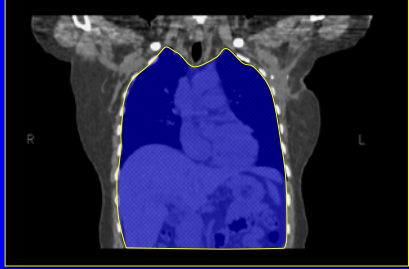
### Tissue Sliding



Deal with different organs individually?

Balter / UM


### Tissue Sliding



Deal with different organs individually?

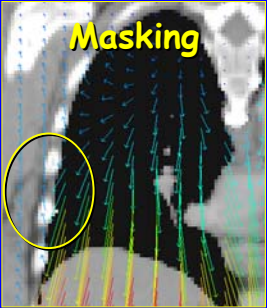
### Segmentation + Registration

No masking



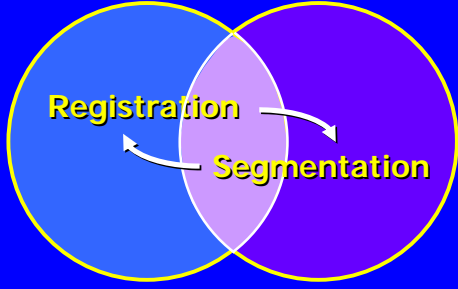
Ribs driven by large lung deformations

Masking



Ribs *not* affected by lung registration


### Registration / Segmentation




Brock / UM

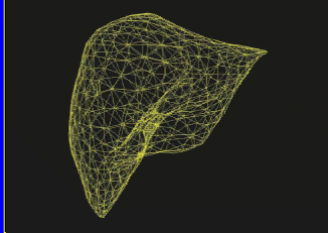
### Finite Element Modeling

Exhale



Inhale

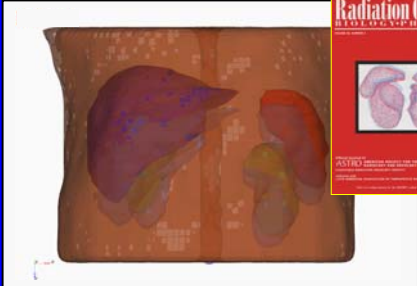





Take into account physical tissue properties (directly)

Brock / PMH

### Finite Element Modeling





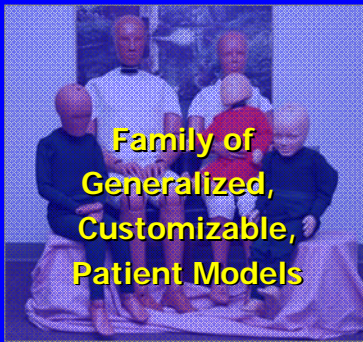
*... thorough segmentation is necessary*

## Deformable Image Registration Methods and Clinical Endpoints

Marc L Kessler, PhD



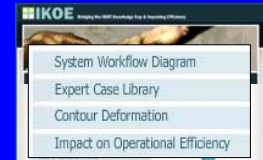
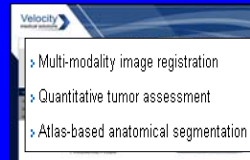
## The Future ?



## Are We Already There?



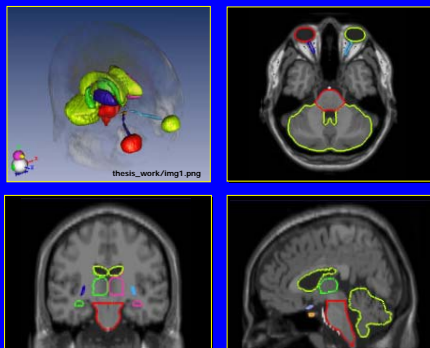
Several independent products are there or *almost* there!



I have no commercial interest in any of these company

## ...from Atlas to Individual

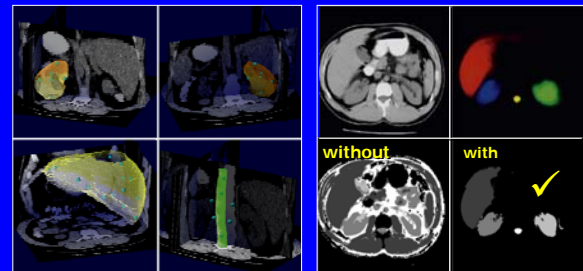
olivier.commowick.org



## Construction of an Abdominal Probabilistic Atlas and its Application in Segmentation

Hyunjin Park, Peyton H. Bland, and Charles R. Meyer\*, Member, IEEE

Meyer/UM

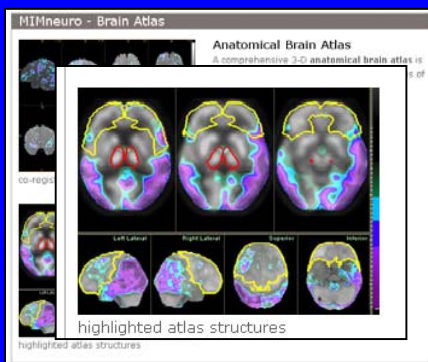


Segment /register / average

Segment using atlas

## ...from Atlas to Individual

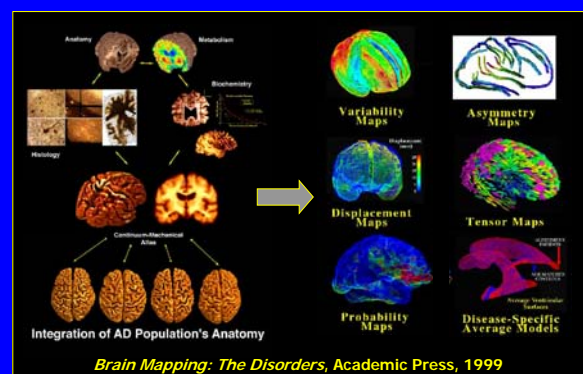
www.mimvista.com



I have no commercial interest in this company!

## ...from Individuals to Atlas

Thompson / UCLA



Brain Mapping: The Disorders, Academic Press, 1999

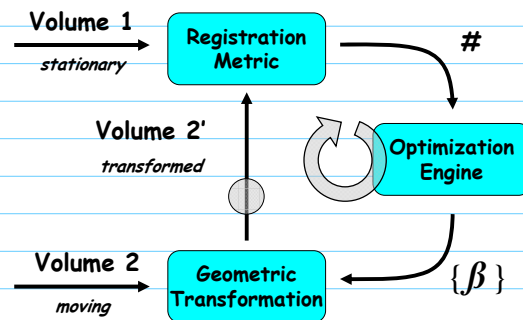
# Deformable Image Registration Methods and Clinical Endpoints

Marc L Kessler, PhD

## Let's Recap

- ✓ The geometric transformation  $T$   
Affine / *not*-Affine
- ✓ The Registration Metric  
Geometry / Intensity
- ✓ Optimization Engine  
Interactive / Automated

## Recipe for Image Registration



## Recipe for Image Registration

2 Image Volumes

1 Transformation Model

1 Registration Metric

1 Optimization Engine

→ n Evaluation Tools

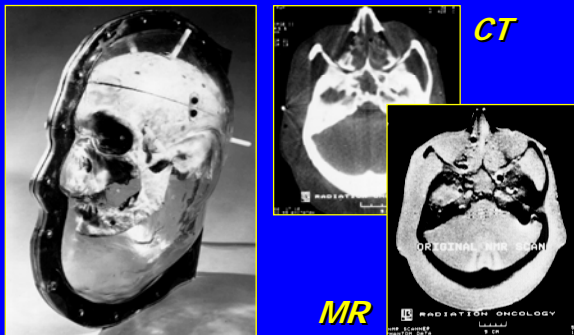
## Evaluation Tools

How do we know how well these registration methods perform?

- build phantoms and test them  
*we can know the truth!*
- provide tools to examine results  
*we don't know the truth!*

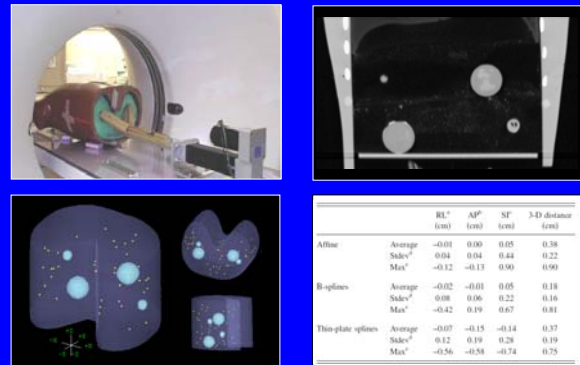
## Multimodality Phantoms

Circa 1986



## 4D Phantoms

Kashani / UM

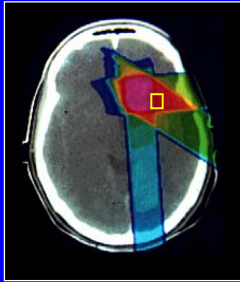


# Deformable Image Registration Methods and Clinical Endpoints

Marc L Kessler, PhD

## Evaluation Tools

### Visualization Tools



- Color gel or wash overlay
- Split /dual screen displays
- Anatomic boundary overlay!

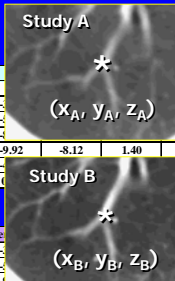
## Evaluation Tools

### Numerical Tools

Point	Description	Exhale		Z
		X	Y	
1	2nd branch of bronchial tree	-5.37	0.98	-2.92
2	3rd branch of bronchial tree	-5.73	2.12	-5.92
3	4th branch of bronchial tree	-6.50	2.77	-9.42
4	Vessel bifurcation 1	-8.12	3.37	-11.42
5	Vessel bifurcation 2	-8.06	-1.95	-3.92
6	Vessel bifurcation 3	-10.69	2.47	1.08

all values in *cm*.

Exhale' (w/ TPS alignment)					ΔZ
-4.71	-0.47				-0.44
-5.35	0.58				0.09
-6.27	0.69				-0.09
-8.19	0.91	-11.60	-0.07	-0.49	-0.18
-7.27	-2.83	-3.63	0.40	0.37	0.29
-10.85	0.87	1.24	-0.07	-0.29	0.16
<b>σ</b>					<b>0.19   0.29   0.26</b>



## AAPM Task Group 132

### Use of Image Registration and Data Fusion Algorithms and Techniques in Radiotherapy

- Methods to assess image registration
- Issues related to accuracy, timing and quality assurance for image registration and fusion

Coming Soon!

## Recipe for Image Registration

- ➡ 2 Image Volumes
- ➡ 1 Transformation Model
- ➡ 1 Registration Metric
- ➡ 1 Optimization Engine
- ➡ n Evaluation Tools

## Caution: The Full Recipe?



- ✓ deformation
- ✓ weight loss
- ✓ resection
- ✓ shrinkage
- ✓ Δ vascular

## Dose Mapping?

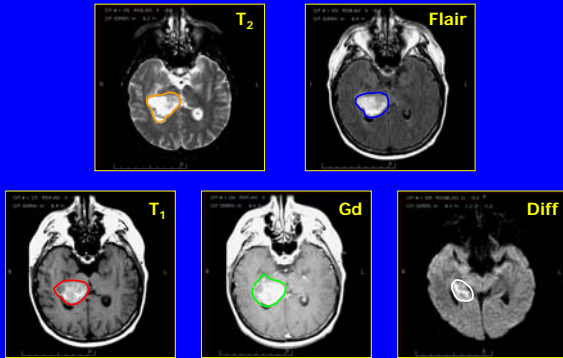
### Dealing with volume elements that may:

- change shape / appear / disappear  
... need proper spatial re-sampling
- don't necessarily add in a linear fashion  
... need some sort of radiobiology
- exist in homogenous intensity regions  
... hard to evaluate registration

# Deformable Image Registration Methods and Clinical Endpoints

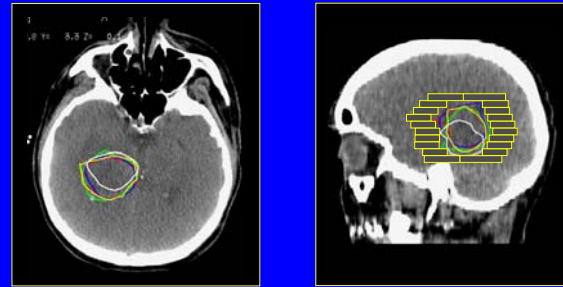
Marc L Kessler, PhD

## Opportunities & Challenges



## More than just mechanics!

What Now ?



MR volumes mapped to CT study

## Summary

- Tools *are* now available to register and integrate image, anatomy & dose for both  $T_x$  planning and  $T_x$  delivery
- These tools can be used to help build better models of the patient and to help customize and adapt therapy
- Work towards more standard and robust tools and validations methods (for non-rigid) situations continues

## Product Comparison

Imaging Technology  
NEW

[www.ITNonline.net](http://www.ITNonline.net)

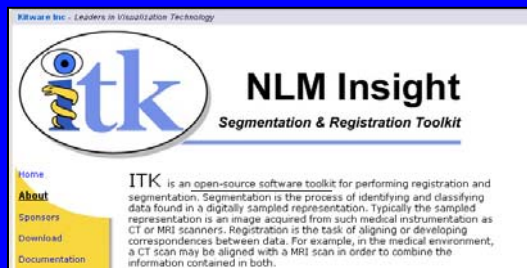


### Comparison Charts

You may compare as many as five (5) products at one time. Please make your selections from the list below and then click on the Submit button. A customized comparison will be generated automatically for you.

- IT Cerberus - Cerberus PET/CT Workstation
- IT CME - Focal Fusion
- IT GE Healthcare - Hawkeye
- IT GE Healthcare - Volumetric - Image Fusion Software, with Image Registration option
- IT GE Healthcare - Volumetric - Image Fusion Software, with Image Registration option and Advantage Windows Workstation
- IT Hermes - HERMES Workstation
- IT Hecate - AVIA- Fusion/ID
- IT MDX - Galileo
- IT MedImage - MedView Volume Registration Package (Macintosh)
- IT MedImage - MedView Volume Registration Package (Windows)

**Don't try this at home!**



[www.itk.org](http://www.itk.org)

**Joint Imaging -Therapy Symposium**  
**Image Processing and Analysis**  
**for Radiotherapy Guidance**

**Deformable Image Registration  
Methods and Clinical Endpoints**

**Marc L Kessler, PhD**