

Purpose: To model the ultrasound effects on cellular calcium ion (Ca²⁺) influx for exploring its potential impact on Ca²⁺ regulated cellular responses to ionizing radiation.

Methods: Based on Silva's membrane electrophysiology model and for the ultrasound (30 ~ 1000mW/cm²) considered, we adopted a linear relation between ultrasound induced cellular membrane strain $\Delta A/A_0$ and ultrasound wave amplitude p as $\Delta A/A_0 \sim p/((\text{Rho} \cdot C) \cdot (\text{Rho} \cdot C))$ (A_0 - undisturbed membrane area, ΔA - stress induced area increase, Rho - liquid density, C - sound velocity). The energy density W associated with membrane strain is proportional $(\Delta A) \cdot (\Delta A)$ while the ultrasound intensity I is proportional to $p \cdot p$ to yield $W(I) = k_w \cdot I$ with a linearity coefficient k_w . Open channel fraction f_0 and rate of exogenous calcium influx q_{in} can be expressed as the following.

$$f_0 = 1/(1+a \cdot \exp(-f_e \cdot k_w \cdot I/(kTN)))$$

$$q_{in} = 4f_0 \cdot P_{max} \cdot V_m F \cdot F/(RT)(C_{aex} - C_{ac} \cdot \exp(2FV_m/(RT)))/(1 - \exp(2FV_m/(RT)))$$

(a - probability that a channel is in open state without load, f_e - fraction of strain energy used to gate the channel, k - Boltzmann constant, T - temperature, N - area channel density, P_{max} - membrane's ionic permeability when all channels are open, V_m - membrane potential, F - Faraday's constant, R - gas constant, C_{aex} - extracellular calcium concentration, C_{ac} - cytosolic free calcium concentration)

Results: A sigmoid relationship between q_{in} and I is obtained, which is due to the Boltzmann character of the mechanosensitive channels. It's shown that a transient rise of q_{in} can be induced at intensities higher than 40 mW/cm² and stimulation over 1200 mW/cm² would lead to unphysiological level of intracellular Ca²⁺.

Conclusions: The calcium transient induced by low-intensity ultrasound has been shown to be comparable to that induced by ionizing radiation reported in literatures. Further investigation is thus needed to examine the potential impact of ultrasound on cellular responses to ionizing radiation, such as bystander effect.